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Computation of the available power of a down-regulated wind farm through a Markov Chain Monte Carlo approach

Autores: Patricia Cobelli, Bruno López, Andrés Guggeri, Rodrigo Alonso, Álvaro Díaz, Martín Draper, Gabriel Usera
Mayo 2019

Proyecto: Aporte de reserva rotante a través de parques eólicos.

Agencia Nacional de Investigación e Innovación

Fondo Sectorial de Energía, 2017

Código: FSE_1_2017_1_144504



Computation of the available power of a down-regulated wind farm through a Markov Chain Monte Carlo approach

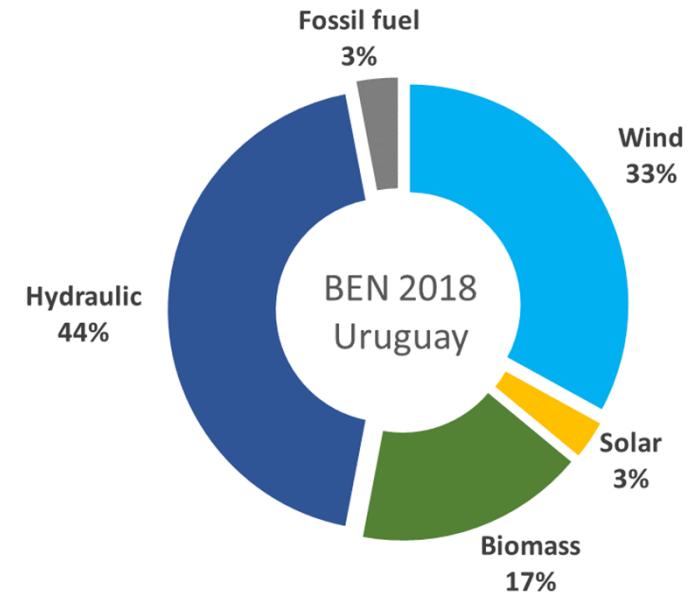
P. Cobelli, B. López, A. Guggeri, R. Alonso, A. Díaz, M. Draper and G. Usera



Motivation

- Wind energy production rapidly increasing participation in electrical market share.
- Challenges to Transmission System Operator
 - Increase electrical power fluctuations
 - Ancillary services to power grid
 - Down-regulated operation (APC)
 - Power reserve

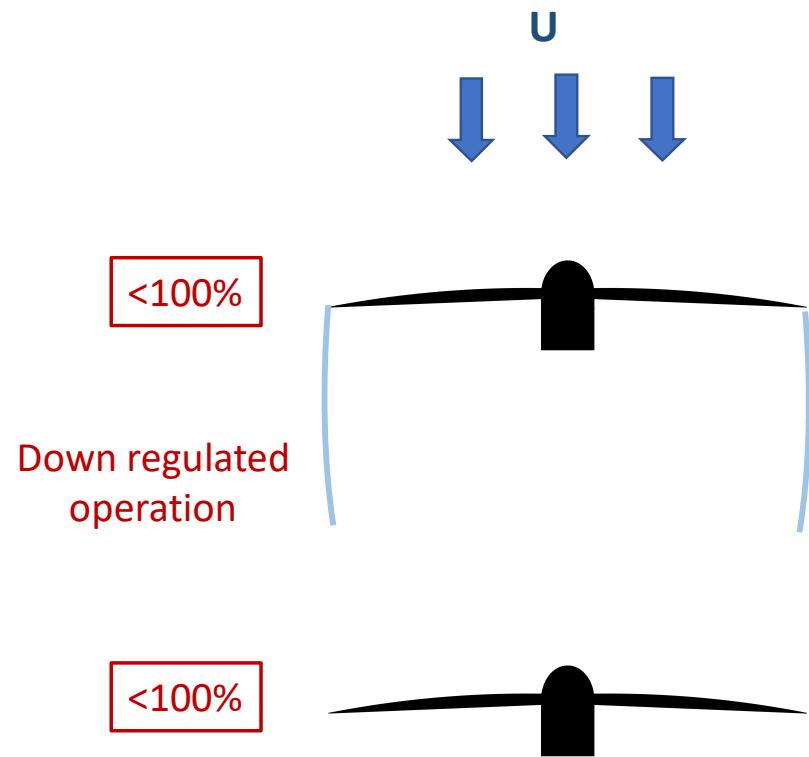
Anual electrical energy production



Outline

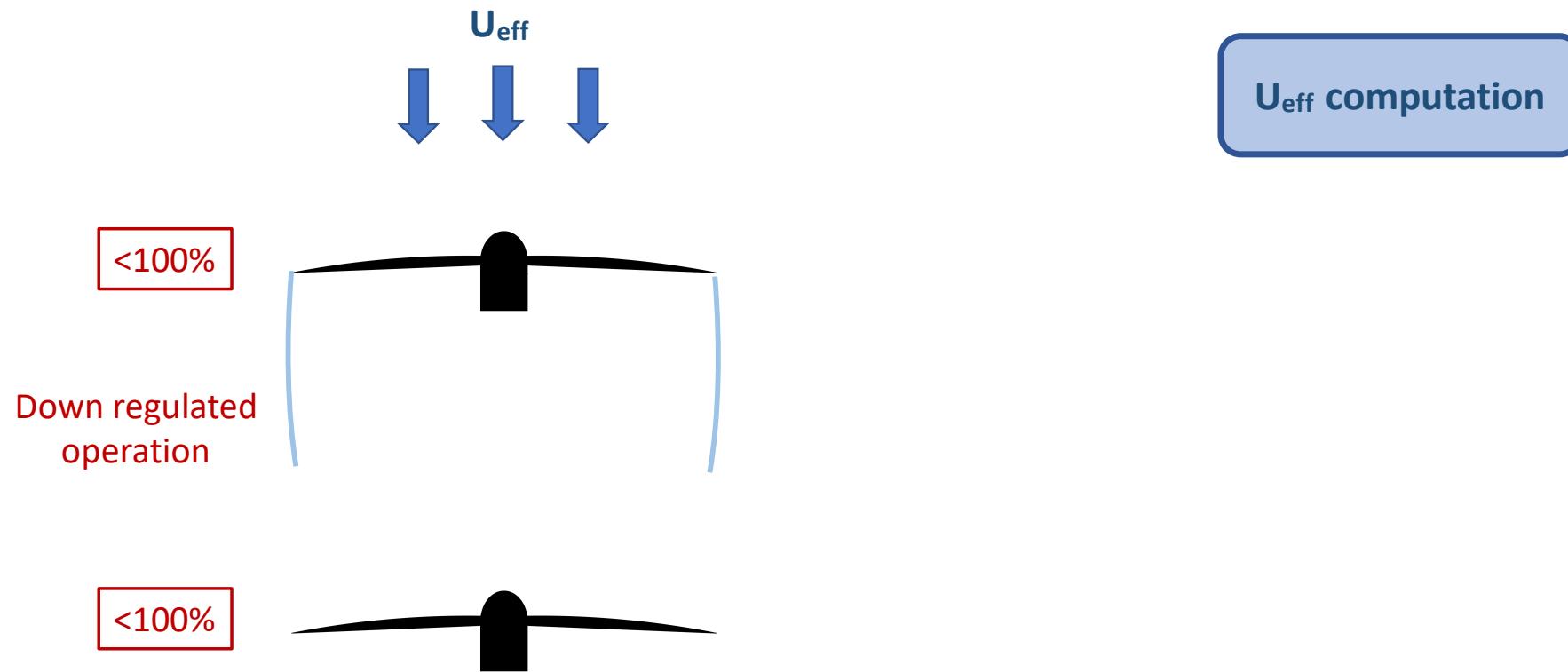
- Methodology
- Validation
- Results
- Conclusions and future work

Methodology I scheme



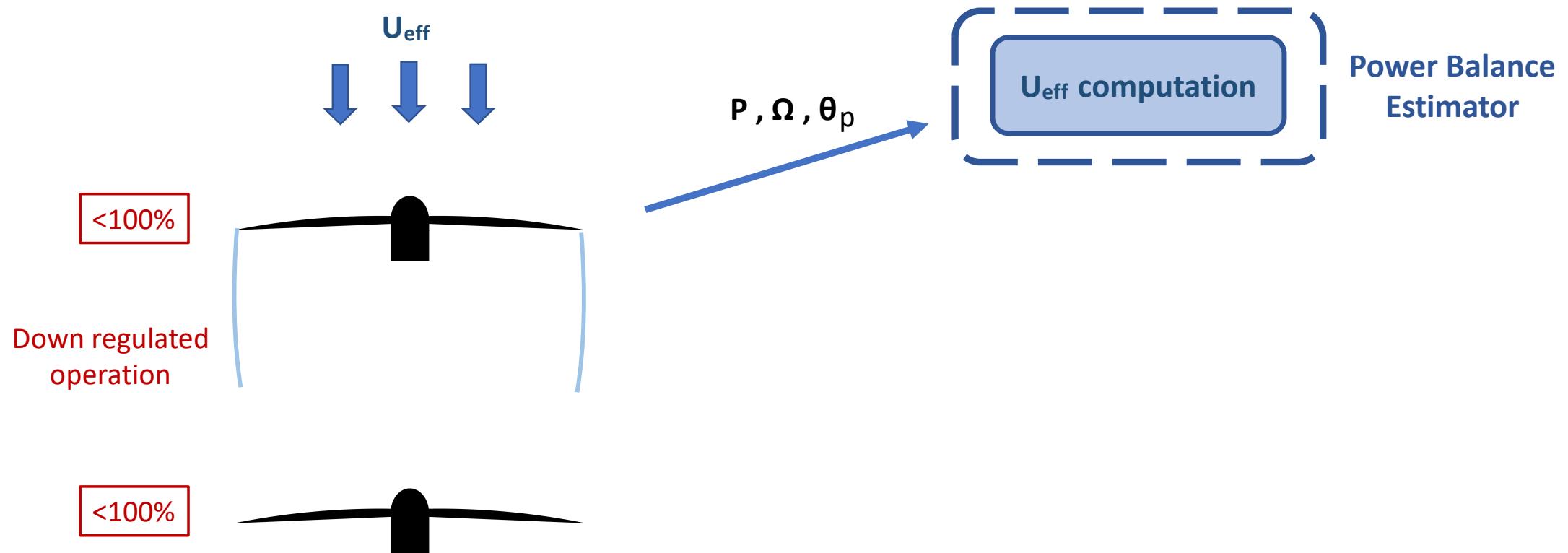
"Possible power of down-regulated offshore wind power plants: The PossPOW algorithm". Göçmen, T. et al. (2018)

Methodology I scheme



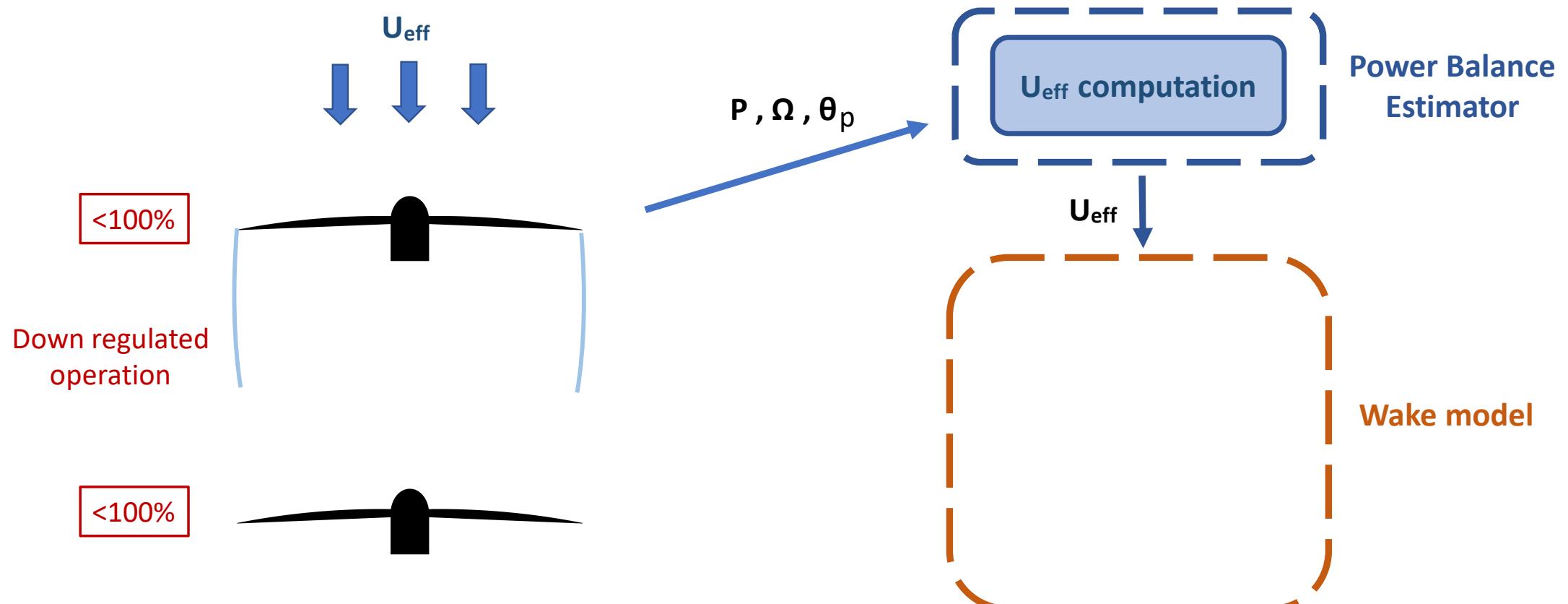
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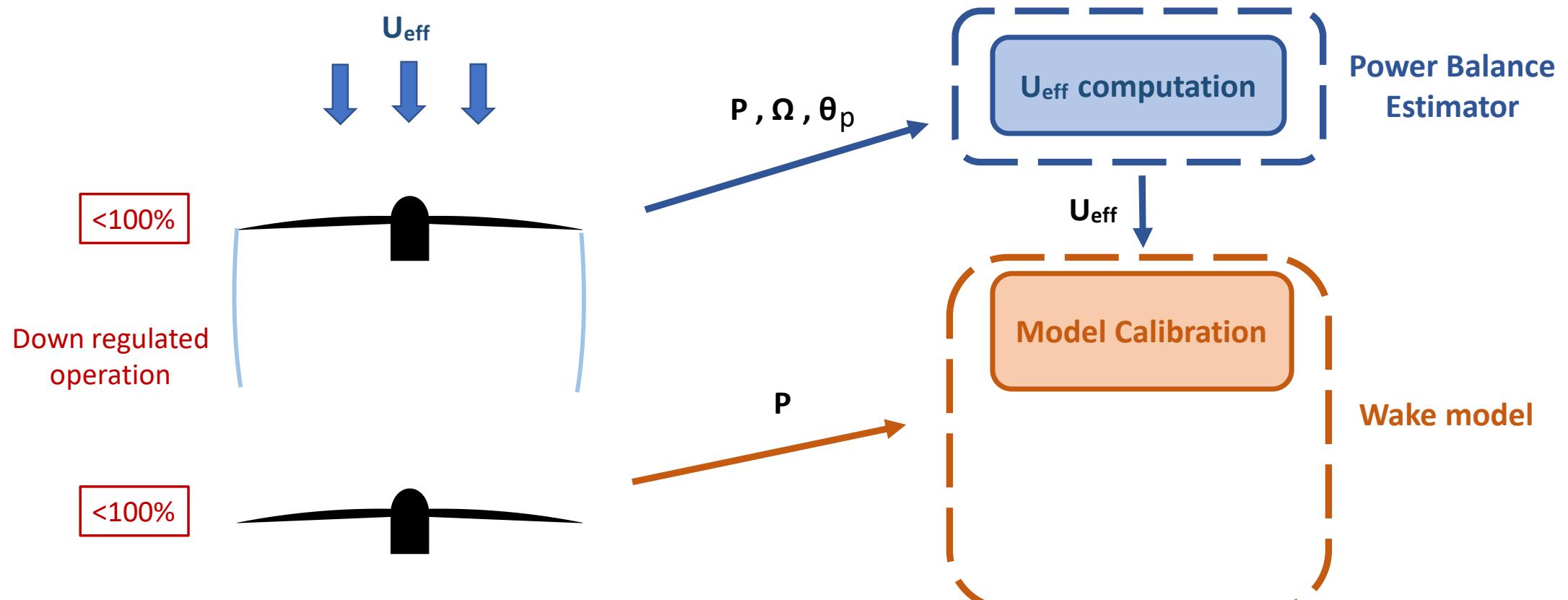
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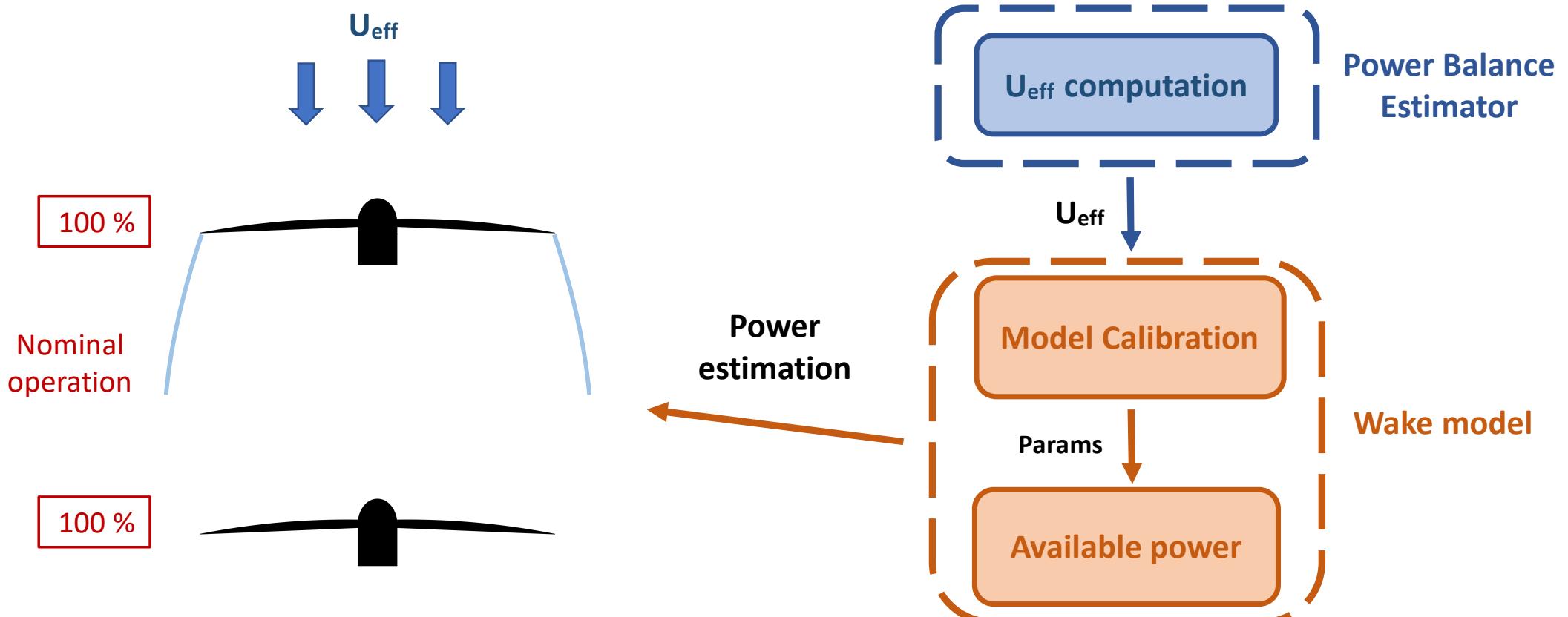
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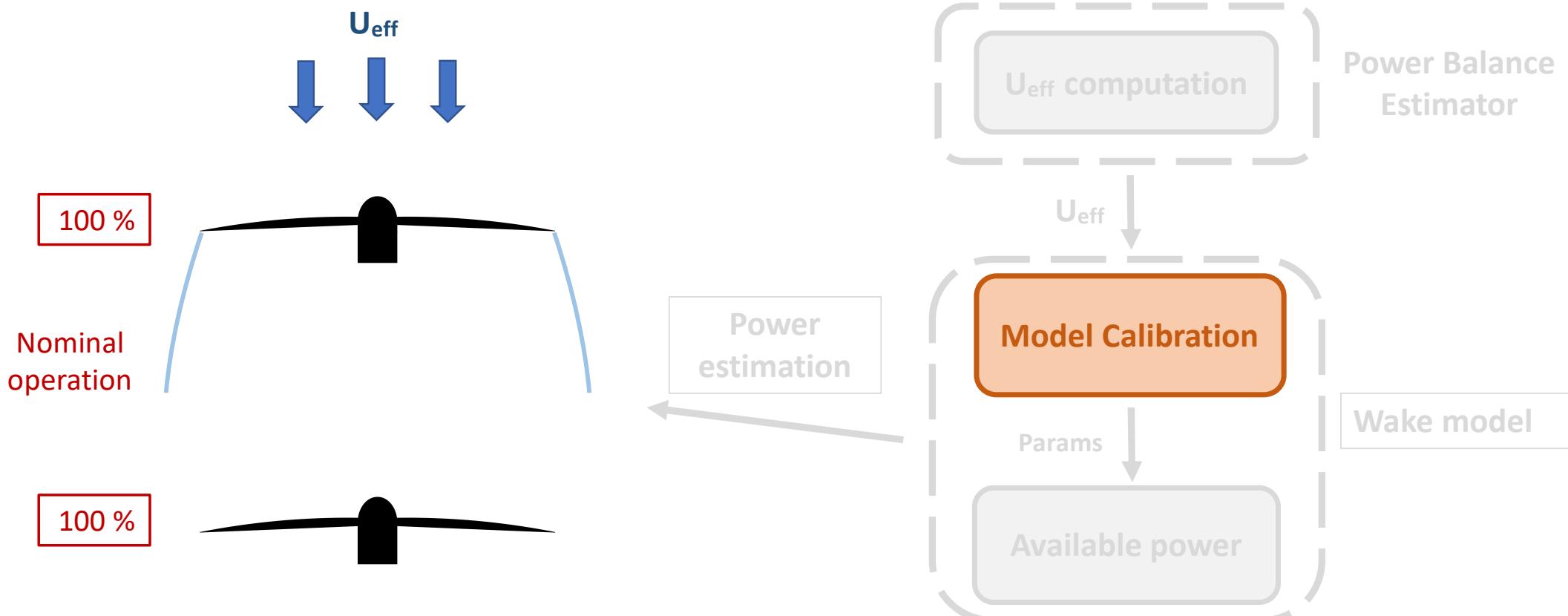
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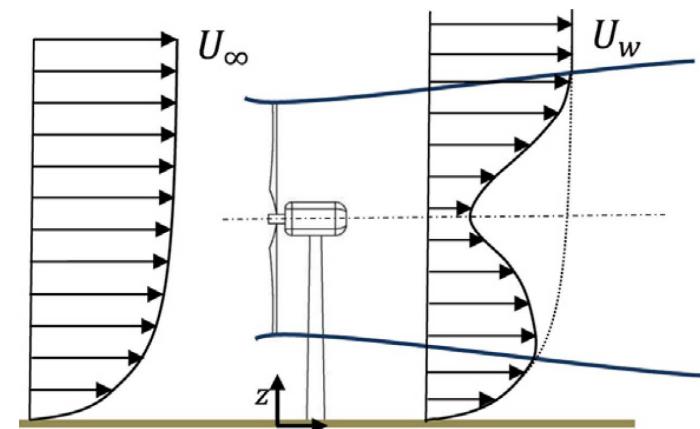
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Methodology | wake model

“A new analytical model for wind-turbine wakes”. Bastankhah M., Porté-Agel F. (2014)

$$\frac{\Delta U}{U_\infty} = \left(1 - \sqrt{1 - \frac{C_T}{8(\sigma/d_0)^2}} \right) \cdot e^{-\frac{(r/d_0)^2}{2(\sigma/d_0)^2}}$$

$$\frac{\sigma}{d_0} = k^* \frac{x}{d_0} + 0.2\sqrt{\beta}$$



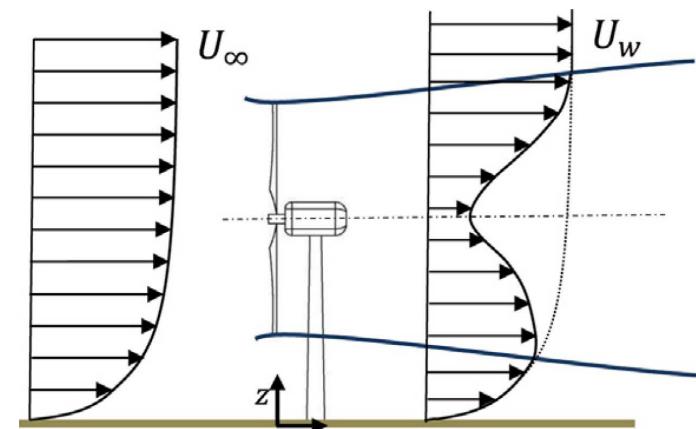
Methodology | wake model

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Needs calibration!!



Methodology I bayesian analysis

Physical system

$$\tilde{P} = g(k^*) + \varepsilon$$

Methodology I bayesian analysis

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Bayesian inference

$$p(k^*|\tilde{P}) = \frac{p(k^*) \cdot p(\tilde{P}|k^*)}{p(\tilde{P})}$$

Methodology I bayesian analysis

Physical system

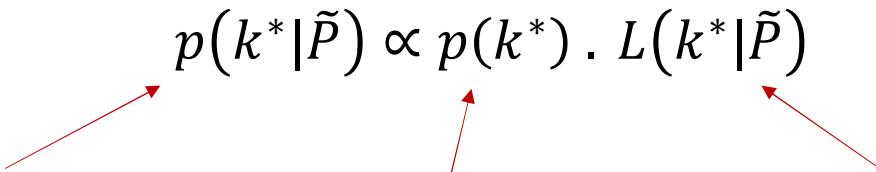
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Bayesian inference

$$p(k^*|\tilde{P}) = \frac{p(k^*) \cdot p(\tilde{P}|k^*)}{p(\tilde{P})}$$

$$p(k^*|\tilde{P}) \propto p(k^*) \cdot L(k^*|\tilde{P})$$

Posterior distribution \propto Prior distribution . Likelihood function



Methodology I likelihood function

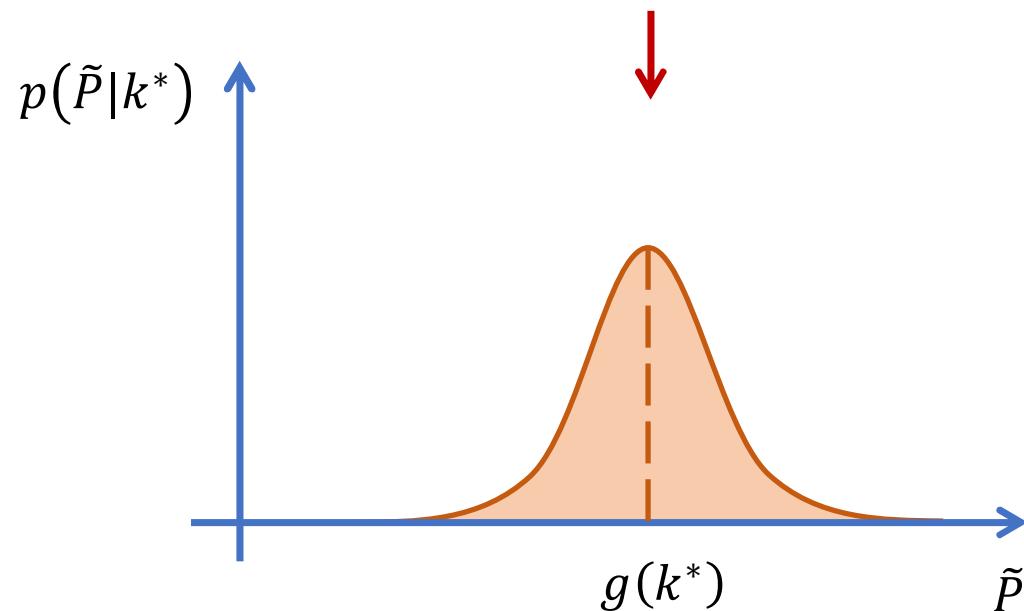
Conditional probability distribution of measurements

$$\tilde{P} = g(k^*) + \varepsilon \quad \rightarrow \quad \varepsilon \sim N(0, \hat{\sigma}^2)$$

Methodology I likelihood function

Conditional probability distribution of measurements

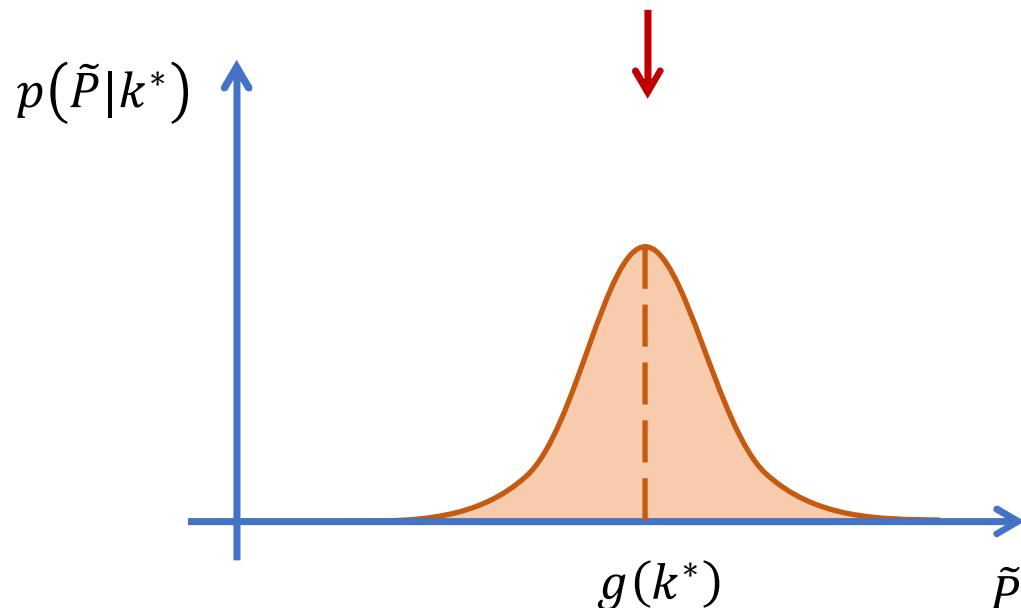
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Methodology I likelihood function

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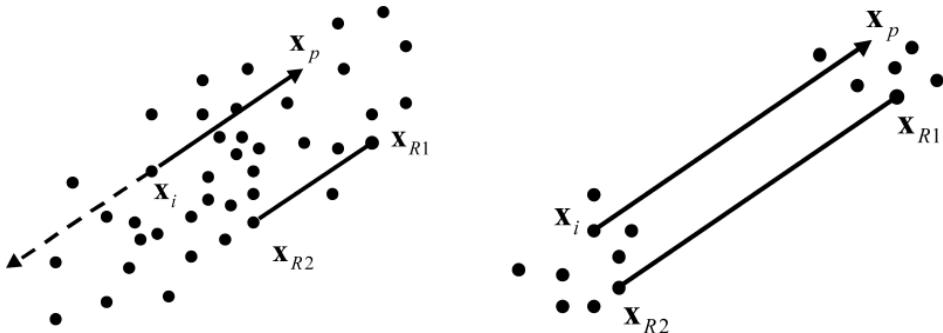
$$e_t(k^*) = \tilde{p}_t - g_t(k^*)$$

$$L(k^*|\tilde{P}, \hat{\sigma}_t^2) = \prod_{t=1}^n \frac{1}{\sqrt{2\pi\hat{\sigma}^2}} \cdot e^{-\frac{1}{2}\left(\frac{e_t(k^*)}{\hat{\sigma}}\right)^2}$$

$$s^2 = \frac{1}{n-1} \sum_{t=1}^n (e_t(k^*))^2$$

Methodology | DREAM

- Markov chain Monte Carlo (MCMC) method for parameters sampling using the posterior distribution.
- Based on the Differential Evolution Markov Chain method.
- Multi chain method: parallel sampling trajectories.

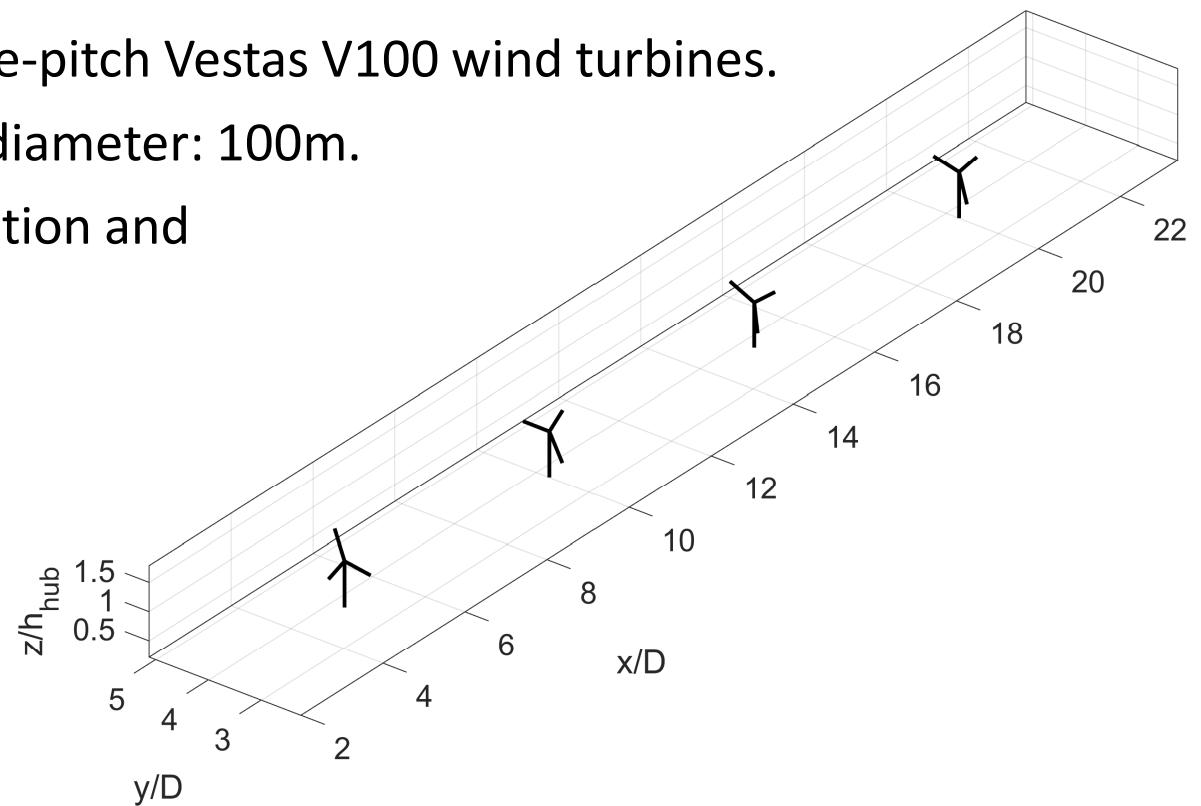


$$p_{acc} = \min \left(1, \frac{p(X_p)}{p(X_i)} \right)$$

“Markov chain Monte Carlo simulation using the DREAM software package: Theory, concepts and MATLAB implementation”. Vrugt, J. (2016)

Validation I setup

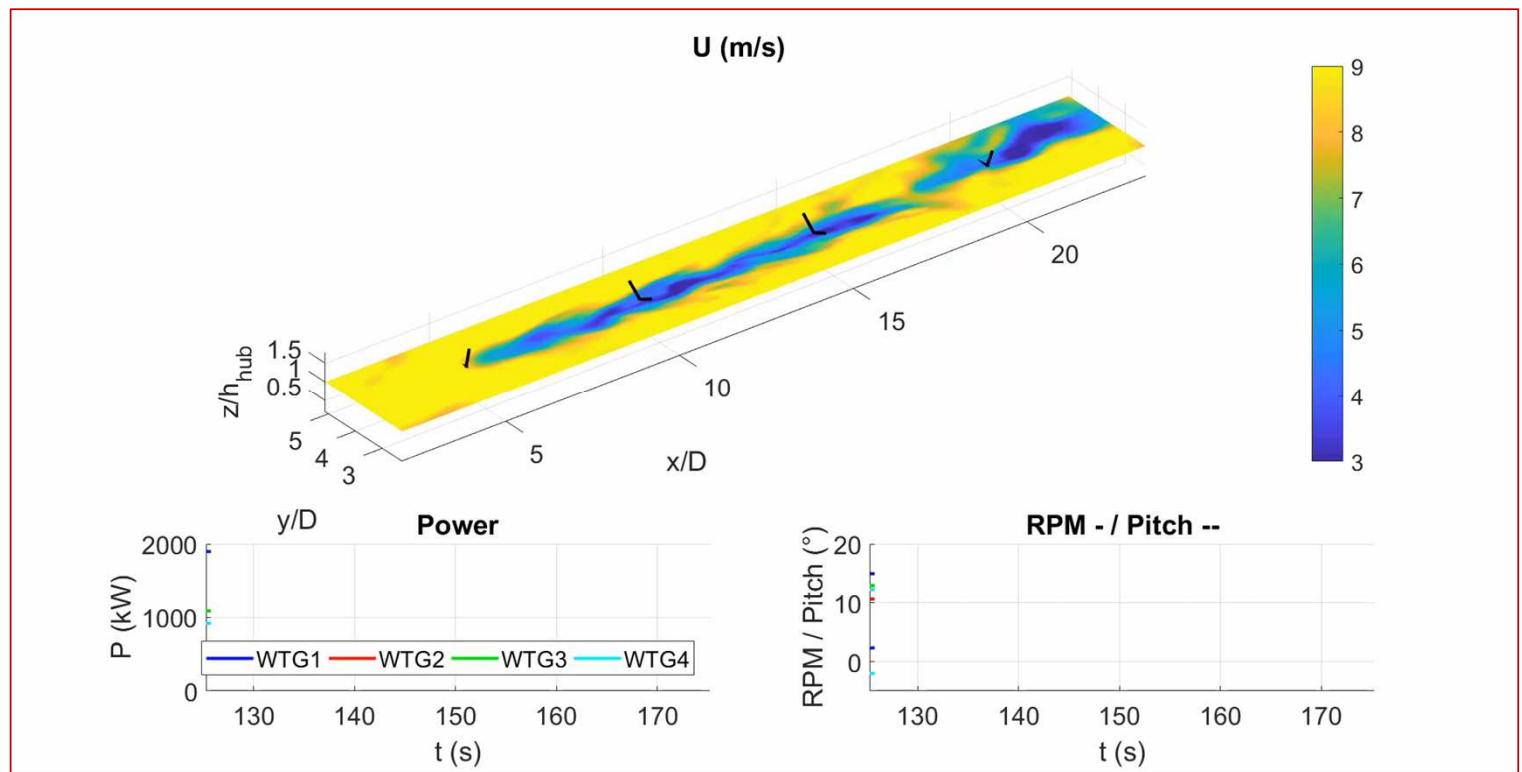
- 7.6 MW wind farm in flat terrain.
- 4 variable-speed, variable-pitch Vestas V100 wind turbines.
- Hub height: 95m. Rotor diameter: 100m.
- Aligned in the wind direction and spaced $5*D$ each other.



Validation | CFD solver

Caffa3d

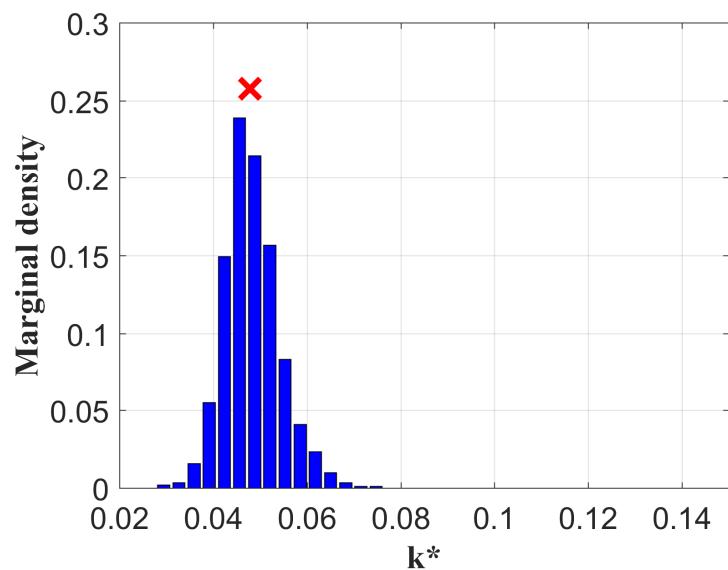
- Finite volumen method
- 2nd order accuracy
- Structured grid blocks
- Parallelization by MPI
- Large Eddy Simulations
- Actuator Line Model
- Pitch and torque control



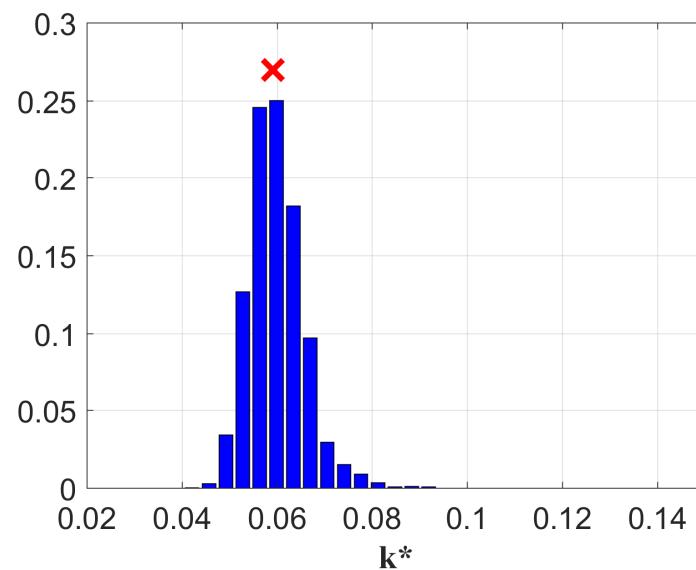
“Simulation of a 7.7 MW onshore wind farm with the Actuator Line Model”. Guggeri, A. et al. (2017)

Results | calibration

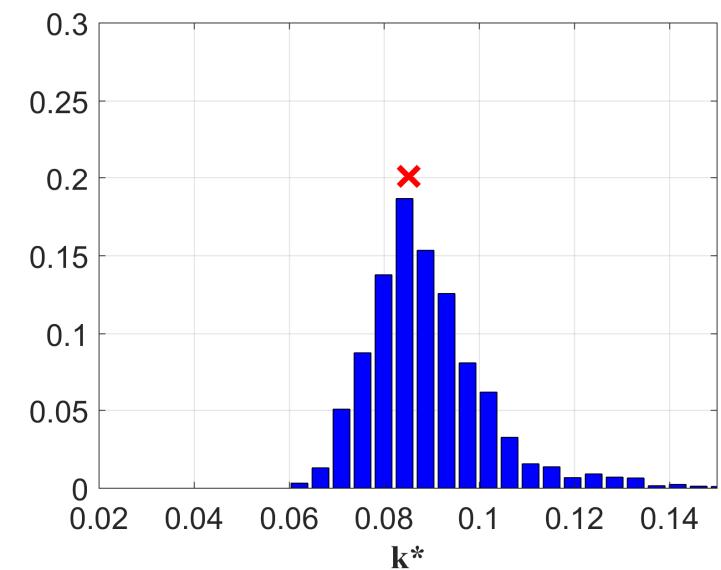
1st WT



2nd WT



3rd WT



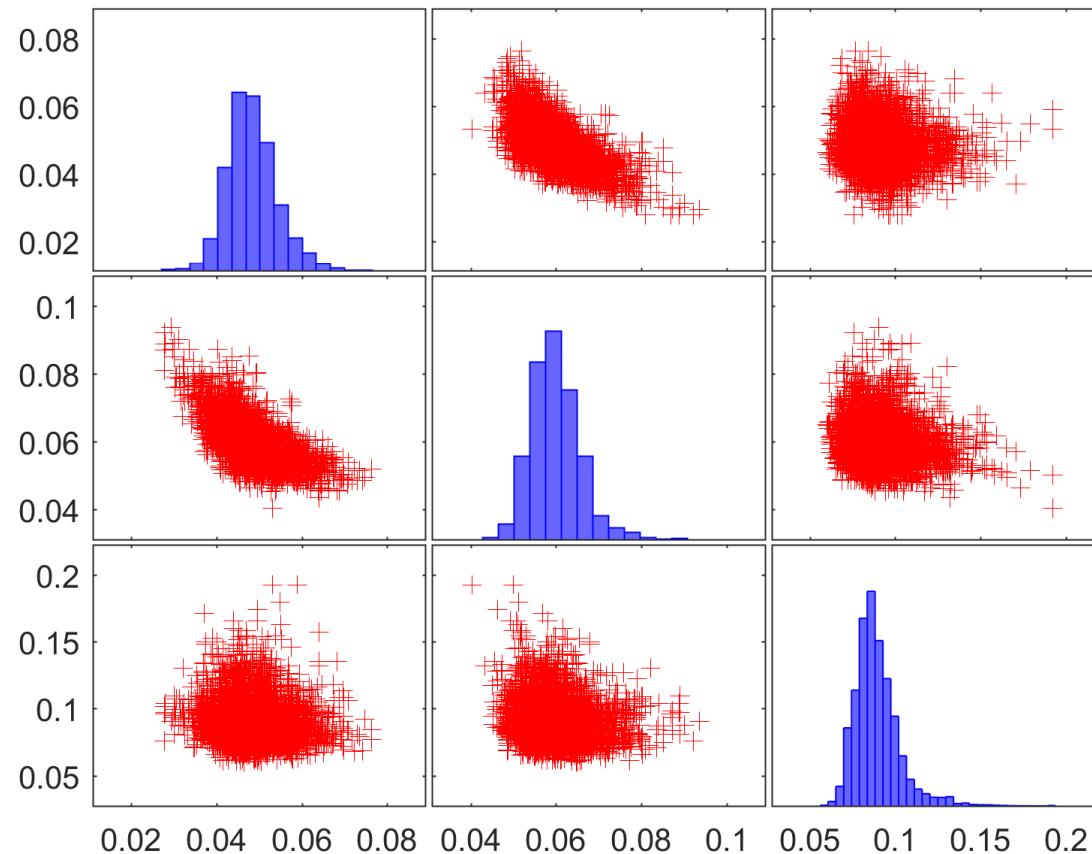
$$k^* = 0,045$$

$$k^* = 0,059$$

$$k^* = 0,085$$

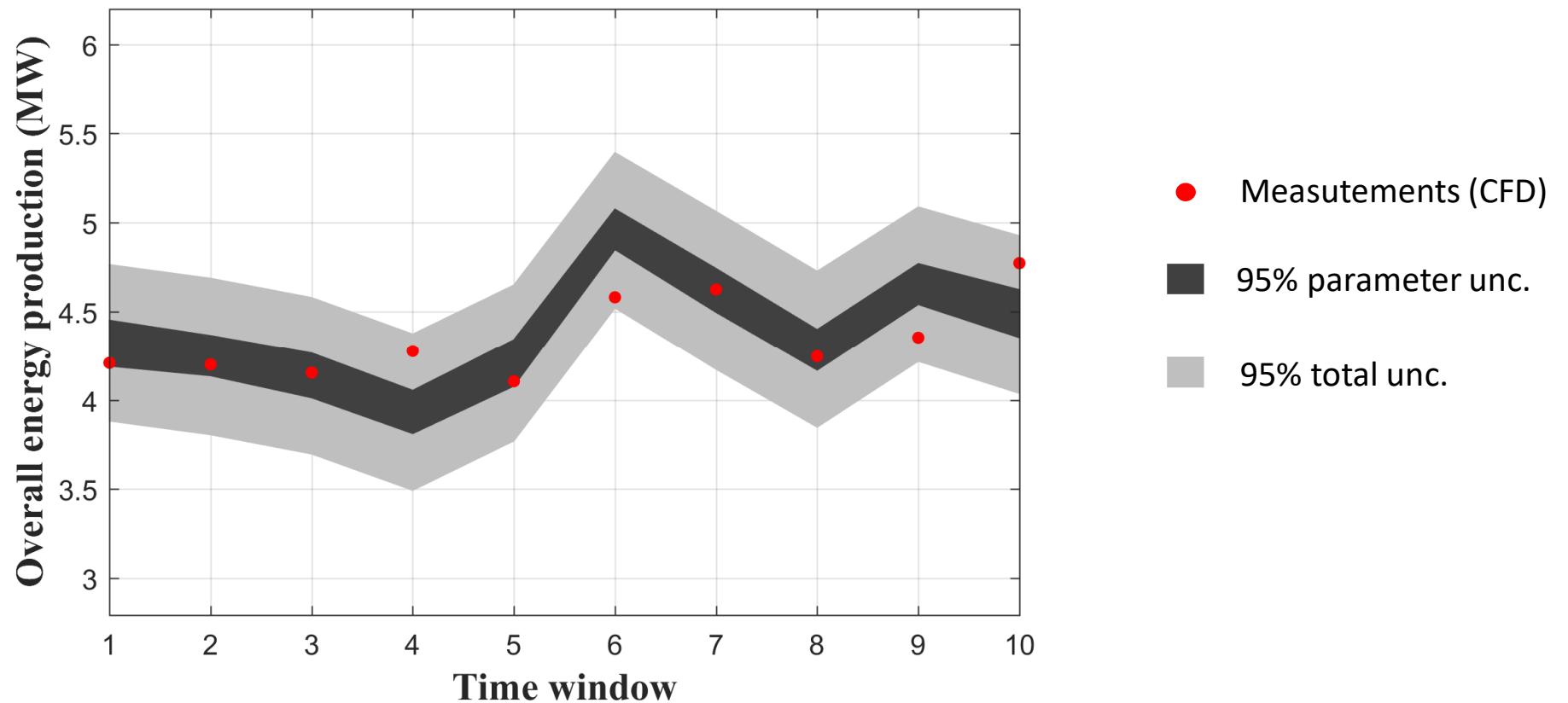
Results I calibration

Two-dimensional correlation plots of posterior parameter samples

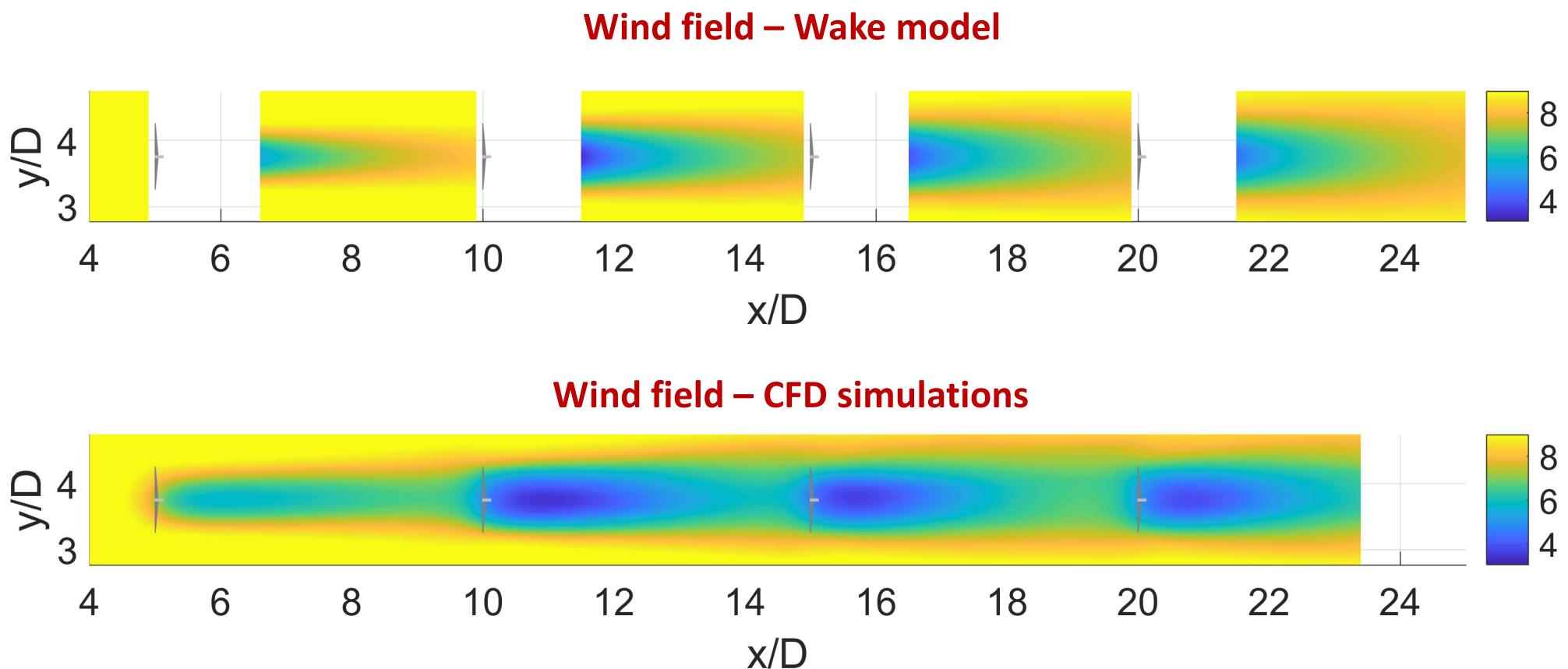


Results I calibration

Down-regulated wind farm at 70%

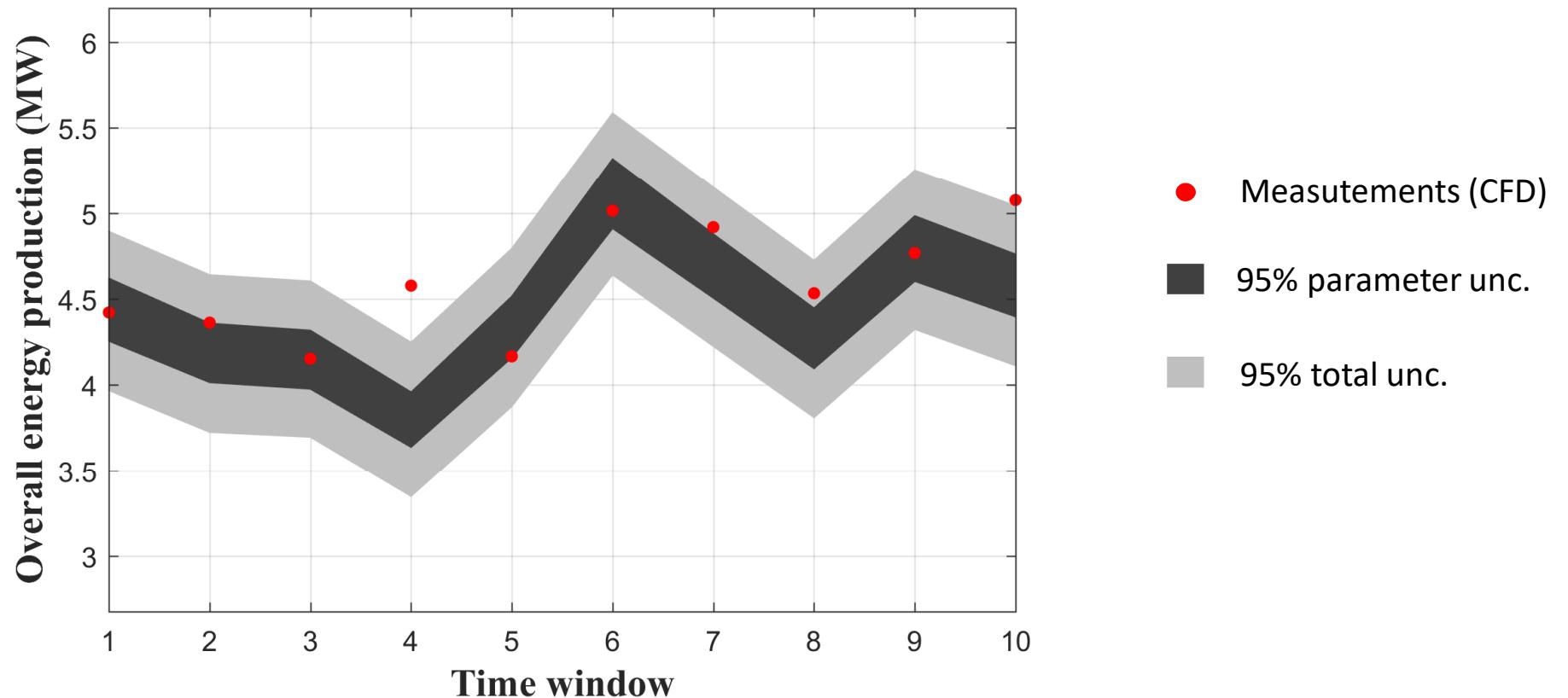


Results I validation



Results I validation

Available power estimation vs. Wind farm at 100%



Conclusions

- The methodology presents overall good results.
- Satisfactory implementation of bayesian analysis techniques for parameter calibration.
- Precise estimation of model uncertainties.

Future work

- Explore DREAM parallelization features
- Evaluate other wake models or mid-Fidelity models
- Explicit dependence on turbulence intensity
- GPU programming



Thank you for your attention!